

Pour $a \geq 0$ et $b > 0$, on a :

$$(\sqrt{a})^2 = a$$

$$\sqrt{a} \times \sqrt{b} = \sqrt{a \times b}$$

$$\frac{\sqrt{a}}{\sqrt{b}} = \sqrt{\frac{a}{b}}$$

Simplifier

Exercice 1 *

Donner la valeur exacte de chacun des nombres :

$$a = \sqrt{25} = 5 ; \quad b = \sqrt{36} = 6 ; \quad c = \sqrt{9} = 3 ; \quad d = \sqrt{100} = 10 ; \quad e = \sqrt{250000} = 500$$

$$f = \sqrt{10^4} = 100 ; \quad g = \sqrt{\frac{4}{9}} = \frac{2}{3} ; \quad h = \sqrt{\frac{25}{100}} = \frac{5}{10} = \frac{1}{2} ; \quad i = \sqrt{49} = 7$$

Exercice 2 **

Écrire les nombres sous la forme $a\sqrt{b}$ où a et b sont des entiers, b positif le plus petit possible :

Indice : $\sqrt{a^2b} = a\sqrt{b}$

$$a = \sqrt{50} = \sqrt{5^2 \times 2} = 5\sqrt{2} ;$$

$$b = \sqrt{54} = \sqrt{3^2 \times 6} = 3\sqrt{6} ;$$

$$c = \sqrt{108} = \sqrt{64 \times 2} = 8\sqrt{2} ;$$

$$d = \sqrt{112} = \sqrt{4^2 \times 7} = 4\sqrt{7} ;$$

$$e = \sqrt{48} = \sqrt{4^2 \times 3} = 4\sqrt{3} ;$$

$$f = \sqrt{75} = \sqrt{5^2 \times 3} = 5\sqrt{3} ;$$

$$g = \sqrt{300} = \sqrt{10^2 \times 3} = 10\sqrt{3} ;$$

$$h = \sqrt{56} = \sqrt{2^2 \times 14} = 2\sqrt{14} ;$$

$$i = \sqrt{128} = \sqrt{8^2 \times 2} = 8\sqrt{2} ;$$

$$j = \sqrt{810} = \sqrt{9^2 \times 10} = 9\sqrt{10} ;$$

$$k = \sqrt{1440} = \sqrt{12^2 \times 10} = 12\sqrt{10} ;$$

$$l = \sqrt{242} = \sqrt{11^2 \times 2} = 11\sqrt{2} ;$$

$$m = 2\sqrt{8} = 2\sqrt{2^2 \times 2} = 4\sqrt{2} ;$$

$$n = 3\sqrt{1200} = 3\sqrt{20^2 \times 3} = 60\sqrt{3}$$

Exercice 3 ***

Simplifier l'écriture de chaque nombre :

$$a = \frac{\sqrt{3}}{\sqrt{27}} = \frac{1}{3} ; \quad b = \frac{\sqrt{180}}{\sqrt{20}} = 3 ;$$

$$c = \frac{\sqrt{125}}{\sqrt{500}} = \frac{1}{2} ;$$

$$d = \sqrt{\frac{7}{63}} = \frac{1}{3} ;$$

$$e = \sqrt{\frac{50}{9}} = \frac{5\sqrt{2}}{3} ; \quad f = 3\sqrt{\frac{25}{144}} = \frac{5}{4} ;$$

$$g = \sqrt{\frac{384}{6}} = 8 ;$$

$$h = 4\sqrt{\frac{1}{4}} = 2 ;$$

$$i = \frac{1}{2}\sqrt{\frac{64}{81}} = \frac{4}{9} ; \quad j = \frac{\sqrt{44}}{2} = \sqrt{11}$$

Énoncé

Sommaire